

Semester Two Examination, 2021

Question/Answer booklet

MATHEMATICS
METHODS
UNITS 1&2

SOLUTIONS

Section One:
Calculator-free

 Student name:

|  |  |
| --- | --- |
| Number of additionalanswer booklets used(if applicable): |  |

## Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters

Special items: nil

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number ofquestionsavailable | Number ofquestions tobe answered | Workingtime(minutes) | Marksavailable | Percentageofexamination |
| Section One:Calculator-free | 9 | 9 | 50 | 58 | 35 |
| Section Two:Calculator-assumed | 12 | 12 | 100 | 94 | 65 |
|  |  | **Total** | 100 |

## Instructions to candidates

1. The rules for the conduct of the Western Australian external examinations are detailed in the Year 12 Information Handbook 2021. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in this Question/Answer booklet preferably using a blue/black pen.
Do not use erasable or gel pens.

3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.

4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

5. It is recommended that you do not use pencil, except in diagrams.

6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.

7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section One: Calculator-free 35% (52 Marks)

This section has**eight** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1 (6 marks)

(a) Solve . (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ indicates appropriate methodü obtains two correct solutions |

Let .

(b) (i) Evaluate . (1 mark)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ obtains zero |

 (ii) Hence, or otherwise, factorise . (3 marks)

|  |
| --- |
| Solution |
| By inspection: |
| Specific behaviours |
| ✓ uses result from (b) to obtain one factorü obtains quadratic factorü completes factorisation |

Question 2 (5 marks)

The quadratic function has roots at and .

(a) Determine the value of the constant and the value of the constant . (3 marks)

|  |
| --- |
| Solution |
| Roots factors:Using last term: |
| Specific behaviours |
| ✓ uses factors to expandü value of ü value of  |

(b) State the range of the function . (2 marks)

|  |
| --- |
| Solution |
| Minimum turning point midway between roots:Hence range is  |
| Specific behaviours |
| ✓ locates turning point or write in T.P. form: ü obtains range |

Question 3 (6 marks)

(a) Evaluate when . (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ obtains ü correct value |

(b) Determine . (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ expands into polynomial or uses product ruleü obtains derivative |

(c) The volume of water in a tank at time seconds is given by cm3. Determine the instantaneous rate of change of volume when seconds. (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ obtains ü correct rate of change with units |

Question 4 (7 marks)

(a) The first term of an arithmetic sequence is and the term is three times the term. Determine the sum of the first terms of this sequence. (4 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ formulates equation involving ü solves for ü correct use of sum formulaü calculates sum |

(b) Determine for the following geometric sequence:

 (3 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ calculates ü correct use of formulaü correct sum to infinity |

Question 5 (7 marks)

(a) Determine the function given that and . (3 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ obtains antiderivative (can have no )ü evaluates constantü states function including their calculated  value |

(b) Determine the equation of the tangent to the curve at the point where . (4 marks)

|  |
| --- |
| Solution |
| Gradient function:Gradient of tangent:-coordinate of point of tangency:Hence tangent: |
| Specific behaviours |
| ✓ obtains gradient functionü calculates gradient of tangentü obtains -coordinateü obtains equation of tangent |

Question 6 (7 marks)

Let .

(a) Sketch the graph of on the axes below. (3 marks)



|  |
| --- |
| Solution |
| See graph |
| Specific behaviours |
| ✓ accurate points for and ü for ü smooth exponential curve |

(b) Solve for . (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ forms equation (✓ correct solution |

(c) Evaluate , giving your answer in simplest surd form without the use of indices.
 (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ eliminates negative indexü correct value as required (accepts ) |

Question 7 (6 marks)

The sum of the first terms of a sequence is given by .

(a) Determine . (1 mark)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ correct value |

(b) Determine , where is the term of the sequence. (2 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ calculates ü calculates  |

(c) Is the sequence arithmetic or geometric? Hence deduce a rule for the term of the sequence. (3 marks)

|  |
| --- |
| Solution |
| The sequence is arithmetic. |
| Specific behaviours |
| ✓ states arithmetic sequenceü calculates common differenceü correct rule |

Question 8 (7 marks)

(a) Solve the equation when . (3 marks)

|  |
| --- |
| Solution |
|  |
| Specific behaviours |
| ✓ indicates ü one correct solutionü second correct solutions |

(b) In triangle , the length of side is cm, and . Determine the length of side . (2 marks)

|  |
| --- |
| Solution |
| Using sin rule: |
| Specific behaviours |
| ✓ indicates correct use of sine ruleü correct length |

(c) Triangle has sides of length and cm. Given that is the longest side in the triangle, determine the value of . (2 marks)

|  |
| --- |
| Solution |
| Using cosine rule: |
| Specific behaviours |
| ✓ indicates correct use of cosine ruleü correct value |

Question 9 (7 marks)

Determine the coordinates of the point(s) where the line intersects the circle with centre and radius .

|  |
| --- |
| Solution |
| Equation of circle:Use line to substitute :Expand:Simplify:Solve quadratic:OrIntersect at the points and . |
| Specific behaviours |
| ✓ writes equation of circleü substitutes line to eliminate or ü expandsü simplifies to form a quadratic equationü solves quadraticü one correct pointü second correct point |

Supplementary page

Question number: \_\_\_\_\_\_\_\_\_

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